

BLANK PAGE

- 1** A factory produces small bottles of natural spring water. Two different machines, X and Y , are used to fill empty bottles with the water. A quality control engineer checks the volumes of water in the bottles filled by each of the machines. He chooses a random sample of 60 bottles filled by machine X and a random sample of 75 bottles filled by machine Y . The volumes of water, x and y respectively, in millilitres, are summarised as follows.

$$\Sigma x = 6345 \quad \Sigma (x - \bar{x})^2 = 243.8 \quad \Sigma y = 7614 \quad \Sigma (y - \bar{y})^2 = 384.9$$

\bar{x} and \bar{y} are the sample means of the volume of water in the bottles filled by machines X and Y respectively.

Find a 95% confidence interval for the difference between the mean volume of water in bottles filled by machine X and the mean volume of water in bottles filled by machine Y . [6]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.

- 2 The number of breakdowns on a particular section of road is recorded each day over a period of 90 days. It is suggested that the number of breakdowns follows a Poisson distribution with mean 3.5. The data is summarised in the table, together with some of the expected frequencies resulting from the suggested Poisson distribution.

Number of breakdowns per day	0	1	2	3	4	5	6	7	8 or more
Observed frequency	0	5	13	17	21	16	9	5	4
Expected frequency	2.718	9.512	16.646		16.993	11.895		3.469	2.407

- (a) Complete the table. [2]

This image shows a full page of white paper with ten horizontal dashed lines, typical of primary school handwriting practice paper. The lines are evenly spaced and extend across the entire width of the page. There is no text or other markings on the paper.

- (b)** Carry out a goodness of fit test, at the 10% significance level, to determine whether or not $Po(3.5)$ is a good fit to the data. [6]

This image shows a full page of primary-ruled paper. It contains ten identical horizontal rows. Each row is defined by three evenly spaced dotted lines, creating a structured space for handwriting practice. The paper is otherwise blank, with no margins or additional markings.

- 3 Toby has a bag which contains 6 red marbles and 3 green marbles. He randomly chooses 3 marbles from the bag, without replacement. The random variable X is the number of red marbles that Toby obtains.

(a) Find the probability generating function of X . [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

Ling also has a bag which contains 6 red marbles and 3 green marbles. He randomly chooses 2 marbles from his bag, without replacement. The random variable Y is the number of red marbles that Ling obtains. It is given that the probability generating function of Y is $\frac{1}{12}(1 + 6t + 5t^2)$.

The random variable Z is the total number of red marbles that Toby and Ling obtain.

(b) Find the probability generating function of Z , expressing your answer as a polynomial in t . [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

- (c) Use the probability generating function of Z to find $\text{Var}(Z)$. [4]



where a , b and c are constants.

The upper quartile of X is equal to 4.

-
- This image shows a full page of white paper with horizontal dashed lines, typical of primary-ruled notebook paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- (b)** Find the exact value of the median of X . [3]

This image shows a full page of blank handwriting practice paper. It features ten sets of horizontal lines, each consisting of three parallel lines: a solid top line, a dashed middle line, and a solid bottom line. These lines are evenly spaced across the entire page, providing a guide for letter height and placement. The background is plain white, and there are no margins or additional markings.

- (c) Find $E(\sqrt{X})$, giving your answer correct to 2 decimal places. [3]

[illegible]

- 5 A company is deciding which of two machines, X and Y , can make a certain type of electrical component more quickly. The times taken, in minutes, to make one component of this type are recorded for a random sample of 8 components made by machine X and a random sample of 9 components made by machine Y . These times are as follows.

Machine X	4.0	4.6	4.7	4.8	5.0	5.2	5.6	5.8	
Machine Y	4.5	4.9	5.1	5.3	5.4	5.7	5.9	6.3	6.4

The manager claims that on average the time taken by machine X to make one component is less than that taken by machine Y .

- (a) Carry out a Wilcoxon rank-sum test at the 5% significance level to test whether the manager's claim is supported by the data. [6]

[illegible]

- (b) Assuming that the times taken to produce the components by the two machines are normally distributed with equal variances, carry out a t -test at the 5% significance level to test whether the manager's claim is supported by the data. [9]

This image shows a full page of a handwriting practice worksheet. It consists of multiple rows of horizontal dashed lines spaced evenly down the page, providing a guide for letter height and placement. The background is plain white, and there are no other markings or text present.

Question 5(c) is printed on the next page.

- (c) In general, would you expect the conclusions from the tests in parts (a) and (b) to be the same? Give a reason for your answer. [1]

[illegible]

BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge Assessment International Education Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cambridgeinternational.org after the live examination series.

Cambridge Assessment International Education is part of Cambridge Assessment. Cambridge Assessment is the brand name of the University of Cambridge Local Examinations Syndicate (UCLES), which is a department of the University of Cambridge.